

Grade 6 • Unit 5 • Assessment Guide

Arithmetic in Base Ten

For the Parent or Teacher — What to look for

Unit 5 extends place-value thinking to decimal operations. The deepest understanding shows up in *WHERE THE DECIMAL POINT GOES* — and why.

Problem 1 — Adding/subtracting decimals

- (a) $4.27 + 13.6 = 17.87$.
- (b) $12.5 - 8.347 = 4.153$ (requires regrouping across decimal places).
- (c) $0.4 + 0.06 + 0.009 = 0.469$.
- Watch for: students who right-justify instead of aligning by decimal point (gives $4.27 + 13.6 = 5.63$ if they treat 13.6 as 136 hundredths).

Problem 2 — Why $0.4 + 0.06 \neq 0.10$

- Correct: $0.4 + 0.06 = 0.46$.
- Confusion source: students add the 4 and the 6 in their respective places (4 tenths + 6 hundredths) and erroneously combine.
- Strong: explains that 0.4 is FOUR tenths (40 hundredths) so $40 + 6 = 46$ hundredths.
- Weak: doesn't see why 0.10 is wrong; can't articulate place value.

Problem 3 — 2.3×1.4 two ways

- Area: $2 \times 1 + 2 \times 0.4 + 0.3 \times 1 + 0.3 \times 0.4 = 2 + 0.8 + 0.3 + 0.12 = 3.22$.
- Whole number: $23 \times 14 = 322$. Place decimal: 2 decimal places total in factors $\rightarrow 3.22$.
- Strong: both methods give the same answer AND student explains the decimal placement.
- Weak: the area model misses the 0.12 partial product; or whole-number method gets 322 but the decimal point is misplaced.

Problem 4 — Estimating products

- (a) $0.8 \times 7.4 \approx 6$ (close to 1×7); actual 5.92.
- (b) $12.5 \times 0.04 \approx 0.5$ (close to 12×0.04); actual 0.500.
- Multiplying by less than 1 PRODUCES a smaller result — this is the central insight.
- Strong: estimates BEFORE computing AND articulates that <1 multipliers shrink the product.
- Weak: expects multiplication to always make numbers bigger.

Problem 5 — $147 \div 6$ long division

- Answer: 24.5 (or 24 R 3 if treated as whole-number division).
- Strong: clear setup; brings down digits; handles the remainder by adding a decimal place.
- Weak: gets 24 R 3 and stops without converting to 24.5; or arithmetic errors at each step.

Problem 6 — $12.6 \div 0.4$

- Multiply both by 10: $126 \div 4 = 31.5$. So $12.6 \div 0.4 = 31.5$.
- Strong: scales both numbers up to make a whole-number division.
- Weak: divides 12.6 by 4 (gets 3.15) — forgot to also scale the dividend; or shifts decimal incorrectly.

Problem 7 — $4.32 \div 8$

- 0.54.
- Strong: long division setup with decimal in correct place.
- Weak: gets 5.4 (decimal misplaced) or 54 (no decimal at all).

Problem 8 — Diego's $2.4 \times 0.5 = 12$ error

- Correct: 1.2.
- Diego forgot to place the decimal point (or placed it incorrectly). $24 \times 5 = 120$, but 2.4×0.5 has TWO decimal places in the factors, so 1.20.
- Strong: explains decimal place counting rule.
- Weak: can't fix the answer; just says 'looks wrong'.

Problem 9 — Mai's $0.6 \div 0.2 = 0.3$ error

- Correct: 3 (NOT 0.3).
- Mai treated 'how many 0.2s in 0.6?' as a multiplication or computed 0.6×0.5 by accident.
- Strong: realizes the answer should be the number of 0.2s in 0.6 (3 of them) and that the answer should be GREATER than 1 because divisor < dividend.
- Weak: agrees with Mai or can't articulate why 0.3 is wrong.
- ★ Counterintuitive sign of division: dividing by a number less than 1 produces a LARGER quotient.

Problem 10 — Sami's lunch (\$20, \$3.85/day, 5 days)

- $5 \times \$3.85 = \19.25 . YES, Sami can afford 5 lunches with \$0.75 left over.
- Strong: multiplies correctly AND interprets the result in context.
- Weak: arithmetic error; or computes but doesn't answer the yes/no question.

Problem 11 — Original problem with answer in (0.1, 1)

- Examples: $0.4 \times 0.8 = 0.32$. Or $0.5 \times 1.2 = 0.6$. Any product in (0.1, 1).
- Strong: the answer IS in (0.1, 1); the problem is well-posed.
- Weak: answer outside range; or product chosen randomly without checking.

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